

Package: npem (via r-universe)

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Title Analysis of Cell Proliferation Assays

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Description Analysis of cell proliferation assays with a normal-Poisson mixture model. Broman et al. (1996)
<[doi:10.1016/S0022-1759\(96\)00136-6](https://doi.org/10.1016/S0022-1759(96)00136-6)>.

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BugReports <https://github.com/kbroman/npem/issues>

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npem.em	<i>Fit the normal-Poisson model to data on a cell proliferation assay</i>
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Description

Uses a version of the EM algorithm to fit the normal-Poisson mixture model to data on a cell proliferation assay.

Usage

```
npem.em(
  y,
  ests,
  cells = 10^6,
  n = c(24, 24, 24, 22),
  n.plates = 1,
  use.order.constraint = TRUE,
  maxit = 2000,
  tol = 0.000001,
  maxk = 20,
  prnt = 0
)
```

Arguments

y	Vector of transformed scintillation counts, in lexicographical order (plate by plate and group by group within a plate.)
ests	Initial parameter estimates, as a vector of length $n.groups + 3*n.plates$, of the form $(\lambda's, (a, b, \sigma)'s)$, where λ is the average number of responding cells per 10^6 cells for a group, and (a, b, σ) are the plate-specific parameters.
cells	Number of cells per well. The λ 's will be rescaled to give response per 10^6 cells. This may be either a single number (if all wells have the same number of cells, or 10^6 if one wishes the λ 's to not be rescaled), a value for each plate (vector of length $n.plates$, or a value for each well (a vector of the same length as y).
n	Vector giving the number of wells within each group. This may have length either $n.groups$ (if all plates have the same number of wells per group) or $n.groups*n.plates$.
n.plates	The number of plates in the data.

<code>use.order.constraint</code>	If TRUE, force the constraint $\lambda_0 \leq \lambda_i$ for all $i \geq 1$; otherwise, no constraints are applied.
<code>maxit</code>	Maximum number of EM iterations to perform.
<code>tol</code>	Tolerance to determine when to stop the EM algorithm.
<code>maxk</code>	Maximum k value in sum calculating $E(k y)$.
<code>prnt</code>	If 0, don't print anything; if 1, print the log likelihood at each iteration; and if 2, print the est's and the log lik. at each iteration.

Details

Calculations are performed in a C routine. [I should describe the normal-Poisson mixture model here.]

Value

<code>ests</code>	The estimated parameters in same form as the input argument <code>ests</code> .
<code>k</code>	The estimated number of responding cells per well, $E(k y)$.
<code>ksq</code>	$E(k^2 y)$
<code>loglik</code>	The value of the log likelihood at <code>ests</code> .
<code>n.iter</code>	Number of iterations performed.

Author(s)

Karl W Broman, <broman@wisc.edu>

References

Broman et al. (1996) Estimation of antigen-responsive T cell frequencies in PBMC from human subjects. *J Immunol Meth* 198:119-132
 Dempster et al. (1977) Maximum likelihood estimation from incomplete data via the EM algorithm. *J Roy Statist Soc Ser B* 39:1-38

See Also

[npem.sem\(\)](#), [npem.start\(\)](#), [npsim\(\)](#), [npem.ll\(\)](#)

Examples

```
# get access to an example data set
data(p713)

# analysis of plate3
# get starting values
start.pl3 <- npem.start(p713$counts[[3]],n=p713$n)
# get estimates
out.pl3 <- npem.em(p713$counts[[3]],start.pl3,n=p713$n)
# look at log likelihood at starting and ending points
```

```

npem.ll(p713$counts[[3]],start.pl3,n=p713$n)
npem.ll(p713$counts[[3]],out.pl3$ests,n=p713$n)
  # repeat with great precision, starting at previous endpoint
out.pl3 <- npem.em(p713$counts[[3]],out.pl3$ests,
                  n=p713$n,tol=1e-13)
  # run SEM algorithm to get standard errors
out.sem.pl3 <- npem.sem(p713$counts[[3]],out.pl3,n=p713$n)
round(out.pl3$ests,3)
round(out.sem.pl3$se,3)

# repeat the above for the pair, plates 3 and 4
# get starting values
start.pl34 <- npem.start(unlist(p713$counts[3:4]),n=p713$n,n.plates=2)
# get estimates
out.pl34 <- npem.em(unlist(p713$counts[3:4]),start.pl34,n=p713$n,n.plates=2)
# look at log likelihood at starting and ending points
npem.ll(unlist(p713$counts[3:4]),start.pl34,n=p713$n,n.plates=2)
npem.ll(unlist(p713$counts[3:4]),out.pl34$ests,n=p713$n,n.plates=2)
# repeat with great precision, starting at previous endpoint
out.pl34 <- npem.em(unlist(p713$counts[3:4]),out.pl34$ests,
                  n=p713$n,tol=1e-13,n.plates=2)
# run SEM algorithm to get standard errors
out.sem.pl34 <- npem.sem(unlist(p713$counts[3:4]),out.pl34,n=p713$n,n.plates=2)
round(out.pl34$ests,3)
round(out.sem.pl34$se,3)

```

npem.ll

Calculate the log likelihood for the normal-Poisson model

Description

Calculates the log likelihood at a single point in the parameter space, for the normal-Poisson mixture model with data on a cell proliferation assay.

Usage

```
npem.ll(y, ests, cells = 10^6, n = c(24, 24, 24, 22), n.plates = 1, maxk = 30)
```

Arguments

y	Vector of transformed scintillation counts, in lexicographical order (plate by plate and group by group within a plate.)
ests	Value of the parameters at which to calculate the log likelihood, as a vector of length $n.groups + 3*n.plates$, of the form $(\lambda$'s, (a, b, σ) 's), where λ is the average number of responding cells per 10^6 cells for a group, and (a, b, σ) are the plate-specific parameters.

cells	Number of cells per well. The λ 's will be rescaled to give response per 10^6 cells. This may be either a single number (if all wells have the same number of cells, or 10^6 if one wishes the λ 's to not be rescaled), a value for each plate (vector of length <code>n.plates</code> , or a value for each well (a vector of the same length as <code>y</code>).
n	Vector giving the number of wells within each group. This may have length either <code>n.groups</code> (if all plates have the same number of wells per group) or <code>n.groups*n.plates</code> .
n.plates	The number of plates in the data.
maxk	Maximum k value in sum calculating $E(k y)$.

Details

Calculations are performed in a C routine.

Value

`loglik` The log likelihood function calculated at the point `ests` in the parameter space.

Author(s)

Karl W Broman, <broman@wisc.edu>

References

Broman et al. (1996) Estimation of antigen-responsive T cell frequencies in PBMC from human subjects. *J Immunol Meth* 198:119-132

See Also

[npem.em\(\)](#)

Examples

```
data(p713)
start.p13 <- npem.start(p713$counts[[3]],n=p713$n)
out.p13 <- npem.em(p713$counts[[3]],start.p13,n=p713$n)
npem.ll(p713$counts[[3]],start.p13,n=p713$n)
npem.ll(p713$counts[[3]],out.p13$ests,n=p713$n)
```

npem.sem

Obtain standard errors for the estimates from npem.em

Description

Uses the SEM algorithm to obtain estimated standard errors for the MLEs obtained after fitting the normal-Poisson mixture model to data on a cell proliferation assay.

Usage

```
npem.sem(
  y,
  npem.em.out,
  cells = 10^6,
  start = npem.em.out$ests * 1.05 + 0.001,
  n = c(24, 24, 24, 22),
  n.plates = 1,
  use.order.constraint = TRUE,
  all.se = TRUE,
  tol = 0.000001,
  maxk = 20,
  prnt = 0,
  do.var = TRUE,
  maxit = 1000
)
```

Arguments

<code>y</code>	Vector of transformed scintillation counts, in lexicographical order (plate by plate and group by group within a plate.)
<code>npem.em.out</code>	Output from the function <code>npem.em()</code> .
<code>cells</code>	Number of cells per well. The λ 's will be rescaled to give response per 10^6 cells. This may be either a single number (if all wells have the same number of cells, or 10^6 if one wishes the λ 's to not be rescaled), a value for each plate (vector of length <code>n.plates</code> , or a value for each well (a vector of the same length as <code>y</code>).
<code>start</code>	Starting estimates, some small distance away from the MLE. A vector of the form (λ 's, (a, b, σ)'s).
<code>n</code>	Vector giving the number of wells within each group. This may have length either <code>n.groups</code> (if all plates have the same number of wells per group) or <code>n.groups*n.plates</code> .
<code>n.plates</code>	The number of plates in the data.
<code>use.order.constraint</code>	If TRUE, force the constraint $\lambda_0 \leq \lambda_i$ for all $i \geq 1$; otherwise, no constraints are applied.
<code>all.se</code>	If TRUE, do the full SEM algorithm; if FALSE, ignore the plate-specific parameters (a,b, σ)'s, to get estimated SEs for the λ 's.
<code>tol</code>	Tolerance to determine when to stop the EM algorithm.
<code>maxk</code>	Maximum k value in sum calculating $E(k y)$.
<code>prnt</code>	If 0, don't print anything; if 1, print out (at each step) the rate matrix and which elements have converged.
<code>do.var</code>	If TRUE, calculate the variance-covariance matrix and standard errors; if FALSE, only calculate the full-data information matrix and rate matrix.
<code>maxit</code>	Maximum number of iterations to perform.

Details

Calculations are performed in a C routine. It is important to first run `npem.em()` with a very small value for `tol`, such as 10^{-13} .

Value

<code>infor</code>	The full-data information matrix
<code>rates</code>	The rate matrix ("DM" in Meng and Rubin's notation).
<code>n.iter</code>	Number of iterations performed in calculating the rate matrix.
<code>var</code>	The estimated variance-covariance matrix.
<code>se</code>	The estimated standard errors. (The square root of the diagonal of <code>var</code> .)

Author(s)

Karl W Broman, <broman@wisc.edu>

References

Broman et al. (1996) Estimation of antigen-responsive T cell frequencies in PBMC from human subjects. *J Immunol Meth* 198:119-132
 Dempster et al. (1977) Maximum likelihood estimation from incomplete data via the EM algorithm. *J Roy Statist Soc Ser B* 39:1-38
 Meng and Rubin (1991) Using EM to obtain asymptotic variance-covariance matrices: the SEM algorithm. *J Am Statist Asso* 86:899-909

See Also

[npem.em\(\)](#)

Examples

```
data(p713)
start.p13 <- npem.start(p713$counts[[3]],n=p713$n)
out.p13 <- npem.em(p713$counts[[3]],start.p13,n=p713$n,tol=1e-13)
out.sem.p13 <- npem.sem(p713$counts[[3]],out.p13,n=p713$n)
```

`npem.start`

Obtain approximate starting values for npem.em

Description

Obtains crude starting values, needed for the EM algorithm.

Usage

```
npem.start(
  y,
  cells = 10^6,
  n = c(24, 24, 24, 22),
  n.plates = 1,
  n.groups = 4,
  n.sd = 2,
  cv = 0.33
)
```

Arguments

<code>y</code>	Vector of transformed scintillation counts, in lexicographical order (plate by plate and group by group within a plate.)
<code>cells</code>	Number of cells per well. The λ 's will be rescaled to give response per 10^6 cells. This may be either a single number (if all wells have the same number of cells, or 10^6 if one wishes the λ 's to not be rescaled), a value for each plate (vector of length <code>n.plates</code> , or a value for each well (a vector of the same length as <code>y</code>).
<code>n</code>	Vector giving the number of wells within each group. This may have length either <code>n.groups</code> (if all plates have the same number of wells per group) or <code>n.groups*n.plates</code> .
<code>n.plates</code>	The number of plates in the data.
<code>n.groups</code>	The number of groups. (This is needed here but not elsewhere, because usually I figure it out from <code>n.plates</code> and the length of the argument <code>ests</code> .)
<code>n.sd</code>	Number of SDs above the mean to use as a cutoff
<code>cv</code>	Coefficient of variation (= SD/ave) used in randomizing the starting point; use <code>cv=0</code> to avoid randomization.

Details

[I should describe the algorithm in more detail here.]

Value

<code>ests</code>	The parameter estimates to use as starting values for the EM algorithm, as a vector of length <code>n.groups + 3*n.plates</code> , of the form $(\lambda$'s, (a, b, σ) 's), where λ is the average number of responding cells per 10^6 cells for a group, and (a, b, σ) are the plate-specific parameters.
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Author(s)

Karl W Broman, <broman@wisc.edu>

References

Broman et al. (1996) Estimation of antigen-responsive T cell frequencies in PBMC from human subjects. *J Immunol Meth* 198:119-132

See Also[npem.em\(\)](#)**Examples**

```
data(p713)
start.p13 <- npem.start(p713$counts[[3]],n=p713$n)
out.p13 <- npem.em(p713$counts[[3]],start.p13,n=p713$n,tol=1e-13)
```

npsim

Simulate data for the normal-Poisson mixture model

Description

Simulate data for a single plate using the normal-Poisson mixture model.

Usage

```
npsim(ests, n = c(24, 24, 24, 22))
```

Arguments

ests	Parameter values as a vector for the form $(\lambda_1, \dots, \lambda_n)$, a, b, σ
n	Lengths of the λ groups

Value

k	The simulated numbers of responding cells per well, useful for comparison with those estimated from npem.em() .
y	The simulated transformed scintillation counts, to be used as input for npem.em() .

Author(s)

Karl W Broman, <broman@wisc.edu>

References

Broman et al. (1996) Estimation of antigen-responsive T cell frequencies in PBMC from human subjects. J Immunol Meth 198:119-132

See Also[npem.em\(\)](#)

Examples

```
ests <- c(0.5,1.5,2.5,5,15,5)
n <- c(24,24,22)
dat <- npsim(ests,n)
out <- npem.em(dat$y,ests=ests,n=n)
jitter <- runif(length(dat$k),-0.1,0.1)
plot(dat$k + jitter, out$k, xlab="True no. cells",
      ylab="Estimated no. cells", lwd=2)
plot(dat$y,out$k,type="n",xlab="Response",ylab="Estimated no. cells")
for(i in unique(dat$k))
  points(dat$y[dat$k==i],out$k[dat$k==i],col=i+1,lwd=2)
```

p711

*Data for a limiting dilution assay***Description**

This is data for a limiting dilution assay for a single patient, composed of 6 pairs of plates at 6 different cell concentrations. The data is from the same subject (at the same time) as [p713.2\(\)](#).

Usage

p711

Format

The data is a list with three components:

counts	A list of length 12, each component of which is a vector giving the square-root-transformed scintillation counts for a
cells	A vector of length 12, giving the estimated number of cells per well for each of the 12 plates.
n	Vector of length 4, giving the number of wells per group, which is the same for each plate.

Author(s)

Karl W Broman, <broman@wisc.edu>
<https://github.com/kbroman/npem>

Source

Michael Tigges, Chiron Biocine

See Also

[p713.2\(\)](#), [p711\(\)](#), [npem.em\(\)](#)

p713

Data for a limiting dilution assay

Description

This is data for a limiting dilution assay for a single patient, composed of 6 pairs of plates at 6 different cell concentrations.

Usage

p713

Format

The data is a list with three components:

counts A list of length 12, each component of which is a vector giving the square-root-transformed scintillation counts for a
cells A vector of length 12, giving the estimated number of cells per well for each of the 12 plates.
n Vector of length 4, giving the number of wells per group, which is the same for each plate.

Author(s)

Karl W Broman, <broman@wisc.edu>
<https://github.com/kbroman/npem>

Source

Michael Tigges, Chiron Biocine

See Also

[p713\(\)](#), [p713.2\(\)](#), [npem.em\(\)](#)

p713.2

Data for a limiting dilution assay

Description

This is data for a limiting dilution assay for a single patient, composed of 5 pairs of plates at 5 different cell concentrations. The data is from the same subject (at the same time) as [p713\(\)](#).

Usage

p713.2

Format

The data is a list with three components:

- counts A list of length 10, each component of which is a vector giving the square-root-transformed scintillation counts for a
- cells A vector of length 10, giving the estimated number of cells per well for each of the 10 plates.
- n Vector of length 4, giving the number of wells per group, which is the same for each plate.

Author(s)

Karl W Broman, <broman@wisc.edu>
<https://github.com/kbroman/npem>

Source

Michael Tigges, Chiron Biocine

See Also

[p713\(\)](#), [p711\(\)](#), [npem.em\(\)](#)

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